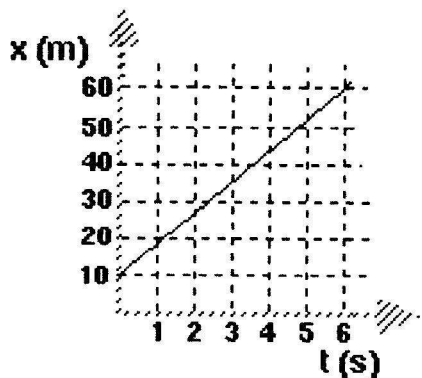


Constant Velocity Particle Model: Review Sheet

1. Consider the following position vs. time graph.



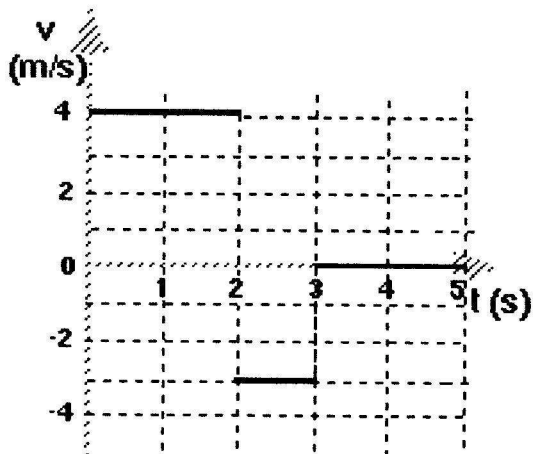
a. Determine the average velocity of the object.

$$8.33 \text{ m/s}$$

b. Write a mathematical model to describe the motion of the object.

$$s = 8.33 \frac{\text{m}}{\text{s}}(t) + 10 \text{ m}$$

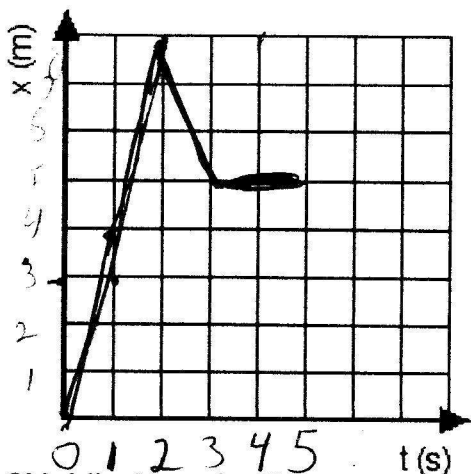
2. Shown below is a velocity vs. time graph for an object.



a. Describe the motion of the object.

0-2 s \rightarrow Forward @ 4 m/s
 2-3 s \rightarrow Reverse @ 3 m/s
 3-5 s \rightarrow stopped

b. Draw a corresponding position vs. time graph. Number the axes. You may assume the object starts from the origin.



c. How far did the object travel in the interval $t = 1$ s to $t = 2$ s?

~~4 m~~ 4 m

d. Find the displacement from $t = 0$ s to $t = 5$ s. Explain how you got your answer.

5 m
 Read 5 @ 5 s
 5 @ 0 s
 $55 - 50$

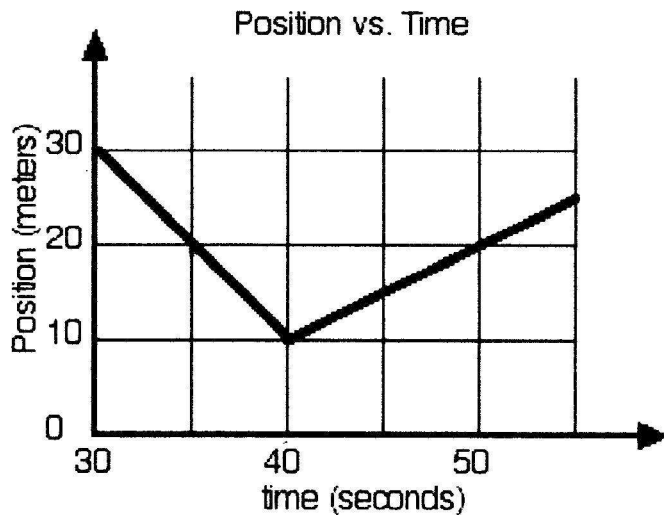
e. Find the average velocity from $t = 0\text{s}$ to $t = 5\text{s}$. Explain how you got your answer.

$$\bar{v} = \frac{\Delta s}{\Delta t} = \frac{5\text{ m}}{5\text{ s}} = 1\text{ m/s}$$

f. Find the average speed from $t = 0\text{s}$ to $t = 5\text{s}$. Explain how you got your answer.

$$\text{Odometer reading} = 8\text{ m} + 3\text{ m} = \frac{11\text{ m}}{5\text{ s}} = 2.2\text{ m/s}$$

3. A bird travels toward the origin, then suddenly reverses direction.



a. Find the average velocity from $t = 30\text{s}$ to $t = 40\text{s}$.

$$\frac{10\text{ m} - 30\text{ m}}{10\text{ s}} = \frac{-20\text{ m}}{10\text{ s}} = -2\frac{\text{m}}{\text{s}}$$

b. Find the average velocity from $t = 40\text{s}$ to $t = 50\text{s}$.

$$\frac{20\text{ m} - 10\text{ m}}{10\text{ s}} = 1\frac{\text{m}}{\text{s}}$$

c. Determine the average speed from $t = 30\text{s}$ to $t = 50\text{s}$.

$$\frac{20\text{ m} + 10\text{ m}}{20\text{ s}} = \frac{30\text{ m}}{20\text{ s}} = 1.5\text{ m/s}$$

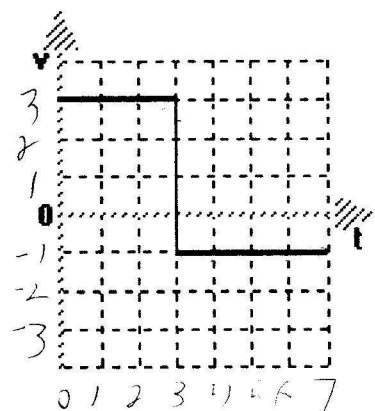
d. Determine the average velocity from $t = 30\text{s}$ to $t = 50\text{s}$.

$$\frac{20\text{ m} - 30\text{ m}}{20\text{ s}} = \frac{-10\text{ m}}{20\text{ s}} = -0.5\text{ m/s}$$

e. Find the velocity at $t = 35\text{ seconds}$.

$$-2\text{ m/s}$$

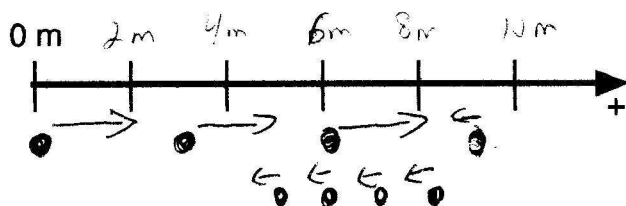
4. A basketball initially travels at 3 meters per second for 3 seconds:



a. Describe the motion of the ball after $t = 3$ seconds.

it travels in the opposite direction at a speed of 1m/s for 4s (velocity = -1m/s)

b. Draw a quantitative motion map that models the motion of the object.



c. How far did the ball travel from $t = 3$ s to $t = 7$ s?

4m

5. A racecar reaches a speed of 95 m/s after it is 450 meters past the starting line. If the car travels at a constant speed of 95 m/s for the next 12.5 s, how far will the car be from the starting line? Use the appropriate mathematical model and show how units cancel.

Given: $s_0 = 450\text{m}$ Unknown = s
 $\bar{v} = 95\text{ m/s}$
 $t = 12.5\text{ s}$

Equation: $\Delta s = \bar{v} t$ \rightarrow or $s = s_0 + v_0 t + \frac{1}{2} a t^2$

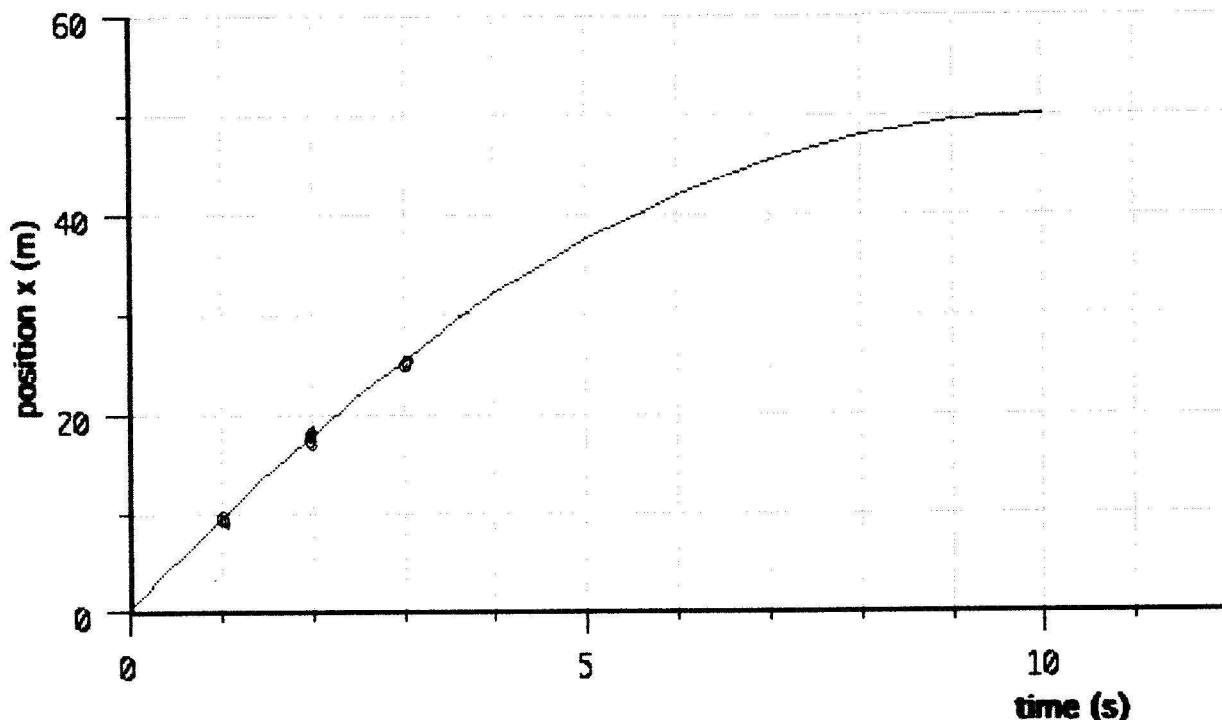
$s - s_0 = \bar{v} t$
 $s = s_0 + \bar{v} t$
 $= 450\text{m} + (95\text{m/s})(12.5\text{ s})$

Substitute
with units

Solve: (you don't need me for this part)

Uniformly Accelerated Particle Model: Review Sheet

Position vs. Time for Object A

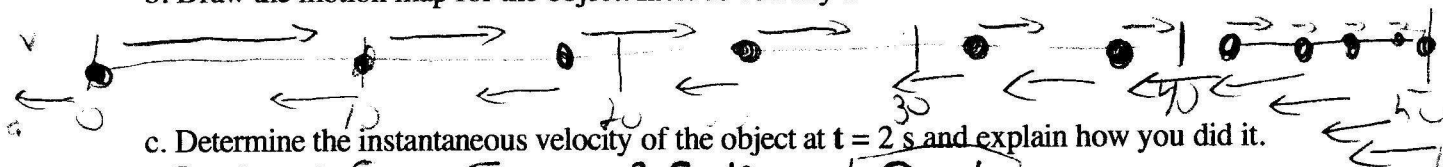


1. Use the graph above to answer the following questions:

a. Give a written description to describe the motion of this object.

Moving in the forward direction and slowing to a stop @ 10 s.

b. Draw the motion map for the object. Include velocity and acceleration vectors.



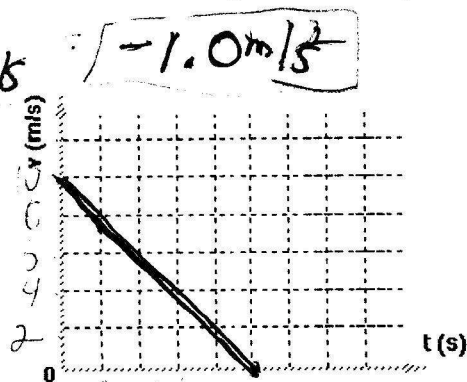
c. Determine the instantaneous velocity of the object at $t = 2$ s and explain how you did it.

$S @ 3s = 26m$ $V_{1-3s} = \frac{26m - 10m}{2s} = 8 m/s$
 $S @ 1s = 10m$ / instant forward @ midpoint = $\sqrt{\text{slope of tangent}}$

d. Assume the initial velocity was 10 m/s; determine the acceleration of the object.

$V_0 = 10 m/s$ $V = V_0 + at$
 $V @ 2s = 7.5 m/s$ $a = \frac{V - V_0}{t} = \frac{7.5 m/s - 10 m/s}{2s} = -1.25 m/s^2$
 $t = 2s$

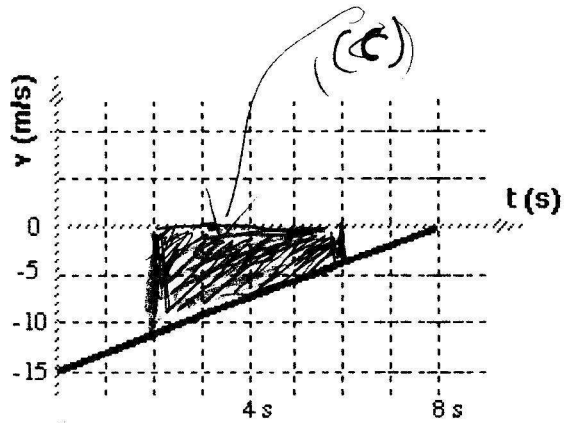
e. Sketch a corresponding velocity time graph for the graph above.



2. Use the graph to answer the following questions.

a. Describe the motion of the object.

Object has initial speed of 15 m/s in reverse direction. It travels in reverse, slowing down until it comes to a stop @ 8 seconds.



b. Determine the acceleration of the object from the graph.

$$a = \frac{\Delta v}{t} \text{ (slope)} = \frac{0 \text{ m/s} - (-15 \text{ m/s})}{8 \text{ s}} = \frac{+15 \text{ m/s}}{8 \text{ s}} = +1.875 \frac{\text{m}}{\text{s}^2}$$

c. Shade the portion of the graph that represents the displacement of the object from 2 to 6 seconds.

d. Use an appropriate mathematical model to calculate the velocity of the object at 2 seconds and at 6 seconds.

$$V = v_0 + at$$

@ 2s: $v = -15 \text{ m/s} + 1.875 \text{ m/s}^2 (2 \text{ s}) = -11.25 \text{ m/s}$

@ 6s: $v = -15 \text{ m/s} + 1.875 \frac{\text{m}}{\text{s}^2} (6 \text{ s}) = -3.75 \text{ m/s}$

e. Use an appropriate mathematical model to calculate the object's displacement from 2 to 6 seconds.

$$\Delta s = \frac{1}{2} (v_0 + v) (t) = \frac{1}{2} (-11.25 \text{ m/s} - 3.75 \text{ m/s}) (4 \text{ s}) = -30 \text{ m}$$

OR

$$\Delta s = v_0 t + \frac{1}{2} a t^2 = (-11.25 \text{ m/s}) (4 \text{ s}) + \frac{1}{2} (1.875 \frac{\text{m}}{\text{s}^2}) (4 \text{ s})^2 = -45 \text{ m} + 15 \text{ m} = -30 \text{ m}$$

3. A car, initially at rest, accelerates at a constant rate of 4.0 m/s^2 for 6 s. How fast will the car be traveling at $t = 6 \text{ s}$?

G) $a = 4.0 \text{ m/s}^2$ U) $v = ?$ E) $v = v_0 + at$ S) $v = 24 \frac{\text{m}}{\text{s}}$

$t = 6 \text{ s}$ S) $v = 0 + (4.0 \frac{\text{m}}{\text{s}^2}) (6 \text{ s})$

$v_0 = 0$

4. A tailback initially running at a velocity of 5.0 m/s becomes very tired and slows down at a uniform rate of 0.25 m/s^2 . How fast will he be running after going an additional 10 meters?

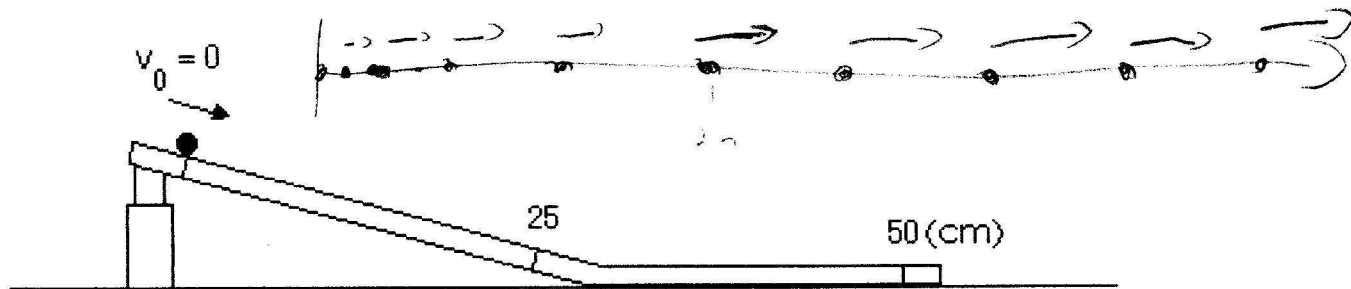
G) $v_0 = 5 \text{ m/s}$ U) $v = ?$ E) $v^2 = v_0^2 + 2a \Delta s$ S) $v = 4.47 \frac{\text{m}}{\text{s}}$

$\Delta s = 10 \text{ m}$ S) $v^2 = (5 \text{ m/s})^2 + 2(-0.25 \frac{\text{m}}{\text{s}^2})(10 \text{ m})$

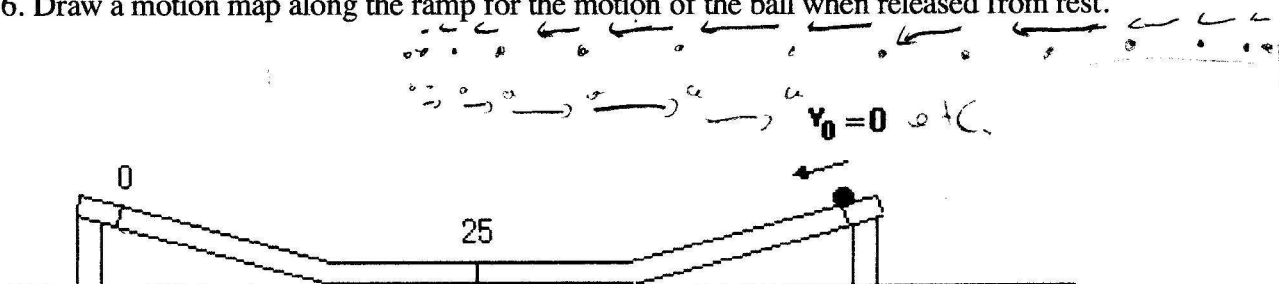
$a = -0.25 \text{ m/s}^2$

↑ Note: sign of a & v are opposite because runner is slowing down

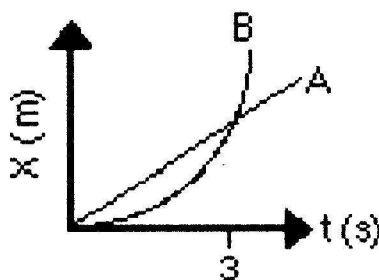
5. Draw a motion map along the ramp for the motion of the ball when released from rest.



6. Draw a motion map along the ramp for the motion of the ball when released from rest.



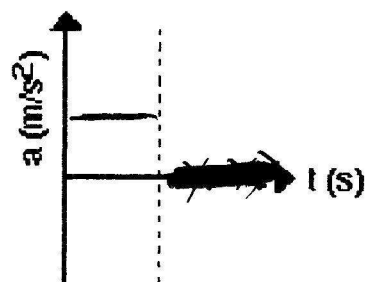
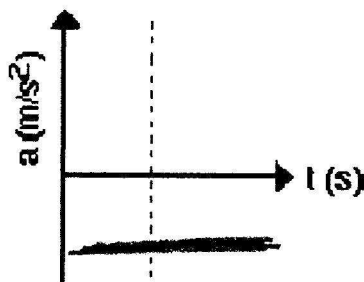
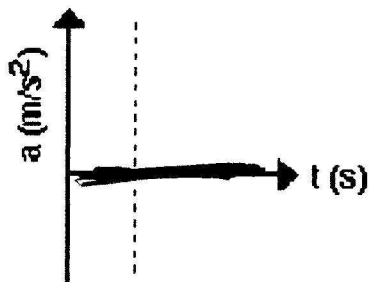
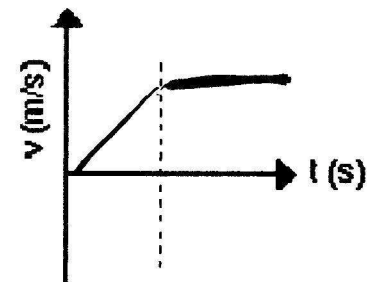
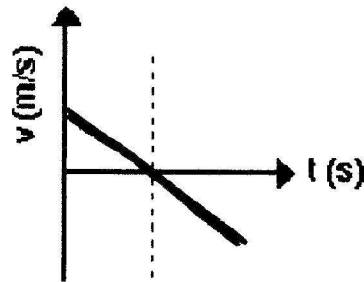
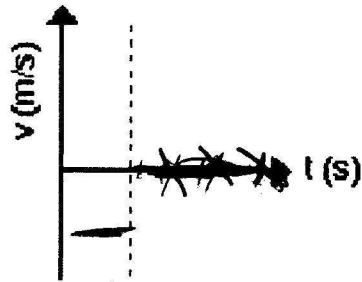
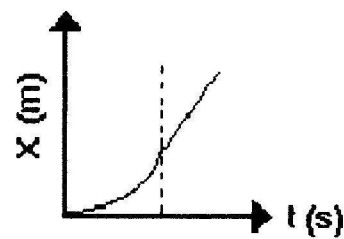
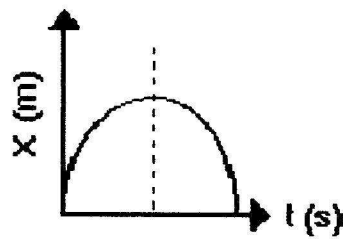
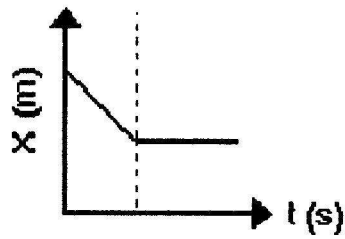
7. Using the graph compare the following quantities for objects A and B. Is $A > B$, $A < B$, or $A = B$.



- a. Displacement from 0 to 3 s $A = B$ How do you know? Both at same point on Y-axis
- b. Displacement from 0 to 1.5 s $A > B$ How do you know? Posit of A vs B on Y
- c. Displacement from 1.5 to 3 s $B > A$ How do you know?)
- d. Average velocity from 0 to 3 s $A = B$ How do you know? Same Δs in same Δt
- e. Average velocity from 0 to 1.5 s $A > B$ How do you know? Greater Disp. for A
- f. Average velocity from 1.5 to 3 s $B > A$ How do you know? Greater for B
- g. Instantaneous velocity at 3 s $B > A$ How do you know? Tan of B > slope of A at 3
- h. Instantaneous velocity at 0 s $A > B$ How do you know? Slope of A > tan of B @ 0

i. If the motion of B is uniformly accelerated, at what time will both graphs have exactly the same slope? Explain.
 at 1.5 s \rightarrow Both have same ave velocity from 0-3 seconds Inst. $v = \text{ave } v$ at midpoint

8. For each of the position vs time graphs shown below, draw the corresponding v vs t , a vs t , and motion map.



Motion Map:

Motion Map:

Motion Map:

